8-1 Study Guide and Intervention *(continued)*

Multiplying Monomials

Powers of Monomials An expression of the form $(x^m)^n$ is called a **power of a power** and represents the product you obtain when x^m is used as a factor n times. To find the power of a power, multiply exponents.

Power of a Power	For any number a and all integers m and n, $(a^m)^n = a^{mn}$.
Power of a Product	For any number a and all integers m and n, $(ab)^m = a^m b^m$.

Example **Simplify $(-2ab^2)^3(a^2)^4$.**

$(-2ab^2)^3(a^2)^4 = (-2ab^2)^3(a^8)$	Power of a Power
$= (-2)^3(a^3)(b^2)^3(a^8)$	Power of a Product
$= (-2)^3(a^3)(a^8)(b^2)^3$	Commutative Property
$= (-2)^3(a^{11})(b^2)^3$	Product of Powers
$= -8a^{11}b^6$	Power of a Power

The product is $-8a^{11}b^6$.

Exercises

Simplify.

1. $(y^5)^2$

2. $(n^7)^4$

3. $(x^2)^5(x^3)$

4. $-3(ab^4)^3$

5. $(-3ab^4)^3$

6. $(4x^2b)^3$

7. $(4a^2)^2(b^3)$

8. $(4x)^2(b^3)$

9. $(x^2y^4)^5$

10. $(2a^3b^2)(b^3)^2$

11. $(-4xy)^3(-2x^2)^3$

12. $(-3j^2k^3)^2(2j^2k)^3$

13. $(25a^2b)^3\left(\frac{1}{5}abc\right)^2$

14. $(2xy)^2(-3x^2)(4y^4)$

15. $(2x^3y^2z^2)^3(x^2z)^4$

16. $(-2n^6y^5)(-6n^3y^2)(ny)^3$

17. $(-3a^3n^4)(-3a^3n)^4$

18. $-3(2x)^4(4x^5y)^2$

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8-2

Study Guide and Intervention

Dividing Monomials

Quotients of Monomials To divide two powers with the same base, subtract the exponents.

Quotient of Powers	For all integers m and n and any nonzero number a, $\frac{a^m}{a^n} = a^{m-n}$.
Power of a Quotient	For any integer m and any real numbers a and b, $b \neq 0$, $\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$.

Example 1 **Simplify $\frac{a^4b^7}{ab^2}$. Assume neither a nor b is equal to zero.**

$\frac{a^4b^7}{ab^2} = \left(\frac{a^4}{a}\right)\left(\frac{b^7}{b^2}\right)$ Group powers with the same base.

$= (a^{4-1})(b^{7-2})$ Quotient of Powers

$= a^3b^5$ Simplify.

The quotient is a^3b^5 .

Example 2 **Simplify $\left(\frac{2a^3b^5}{3b^2}\right)^3$. Assume that b is not equal to zero.**

$\left(\frac{2a^3b^5}{3b^2}\right)^3 = \frac{(2a^3b^5)^3}{(3b^2)^3}$ Power of a Quotient

$= \frac{2^3(a^3)^3(b^5)^3}{(3)^3(b^2)^3}$ Power of a Product

$= \frac{8a^9b^{15}}{27b^6}$ Power of a Power

$= \frac{8a^9b^9}{27}$ Quotient of Powers

The quotient is $\frac{8a^9b^9}{27}$.

Exercises

Simplify. Assume that no denominator is equal to zero.

1. $\frac{5^5}{5^2}$

2. $\frac{m^6}{m^4}$

3. $\frac{p^5n^4}{p^2n}$

4. $\frac{a^2}{a}$

5. $\frac{x^5y^3}{x^5y^2}$

6. $\frac{-2y^7}{14y^5}$

7. $\frac{xy^6}{y^4x}$

8. $\left(\frac{2a^2b}{a}\right)^3$

9. $\left(\frac{4p^4q^4}{3p^2q^2}\right)^3$

10. $\left(\frac{2v^5w^3}{v^4w^3}\right)^4$

11. $\left(\frac{3r^6s^3}{2r^5s}\right)^4$

12. $\frac{r^7s^7t^2}{s^3r^3t^2}$

Lesson 8-2

NAME ______________________________ DATE ____________ PERIOD _____

8-2 Study Guide and Intervention *(continued)*

Dividing Monomials

Negative Exponents Any nonzero number raised to the zero power is 1; for example, $(-0.5)^0 = 1$. Any nonzero number raised to a negative power is equal to the reciprocal of the number raised to the opposite power; for example, $6^{-3} = \frac{1}{6^3}$. These definitions can be used to simplify expressions that have negative exponents.

Zero Exponent	For any nonzero number a, $a^0 = 1$.
Negative Exponent Property	For any nonzero number a and any integer n, $a^{-n} = \frac{1}{a^n}$ and $\frac{1}{a^{-n}} = a^n$.

The simplified form of an expression containing negative exponents must contain only positive exponents.

Example **Simplify $\frac{4a^{-3}b^6}{16a^2b^6c^{-5}}$. Assume that the denominator is not equal to zero.**

$\frac{4a^{-3}b^6}{16a^2b^6c^{-5}} = \left(\frac{4}{16}\right)\left(\frac{a^{-3}}{a^2}\right)\left(\frac{b^6}{b^6}\right)\left(\frac{1}{c^{-5}}\right)$ Group powers with the same base.

$= \frac{1}{4}(a^{-3-2})(b^{6-6})(c^5)$ Quotient of Powers and Negative Exponent Properties

$= \frac{1}{4}a^{-5}b^0c^5$ Simplify.

$= \frac{1}{4}\left(\frac{1}{a^5}\right)(1)c^5$ Negative Exponent and Zero Exponent Properties

$= \frac{c^5}{4a^5}$ Simplify.

The solution is $\frac{c^5}{4a^5}$.

Exercises

Simplify. Assume that no denominator is equal to zero.

1. $\frac{2^2}{2^{-3}}$
2. $\frac{m}{m^{-4}}$
3. $\frac{p^{-8}}{p^3}$
4. $\frac{b^{-4}}{b^{-5}}$
5. $\frac{(-x^{-1}y)^0}{4w^{-1}y^2}$
6. $\frac{(a^2b^3)^2}{(ab)^{-2}}$
7. $\frac{x^4y^0}{x^{-2}}$
8. $\frac{(6a^{-1}b)^2}{(b^2)^4}$
9. $\frac{(3st)^2u^{-4}}{s^{-1}t^2u^7}$
10. $\frac{s^{-3}t^{-5}}{(s^2t^3)^{-1}}$
11. $\left(\frac{4m^2n^2}{8m^{-1}\ell}\right)^0$
12. $\frac{(-2mn^2)^{-3}}{4m^{-6}n^4}$

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8-4 Study Guide and Intervention

Polynomials

Degree of a Polynomial A **polynomial** is a monomial or a sum of monomials. A **binomial** is the sum of two monomials, and a **trinomial** is the sum of three monomials. Polynomials with more than three terms have no special name. The **degree** of a monomial is the sum of the exponents of all its variables. The **degree of the polynomial** is the same as the degree of the monomial term with the highest degree.

Example **State whether each expression is a polynomial. If the expression is a polynomial, identify it as a *monomial, binomial,* or *trinomial.* Then give the degree of the polynomial.**

Expression	Polynomial?	Monomial, Binomial, or Trinomial?	Degree of the Polynomial
$3x - 7xyz$	Yes. $3x - 7xyz = 3x + (-7xyz)$, which is the sum of two monomials	binomial	3
-25	Yes. -25 is a real number.	monomial	0
$7n^3 + 3n^{-4}$	No. $3n^{-4} = \frac{3}{n^4}$, which is not a monomial	none of these	—
$9x^3 + 4x + x + 4 + 2x$	Yes. The expression simplifies to $9x^3 + 7x + 4$, which is the sum of three monomials	trinomial	3

Exercises

State whether each expression is a polynomial. If the expression is a polynomial, identify it as a *monomial, binomial,* or *trinomial.*

1. 36
2. $\frac{3}{q^2} + 5$
3. $7x - x + 5$
4. $8g^2h - 7gh + 2$
5. $\frac{1}{4y^2} + 5y - 8$
6. $6x + x^2$

Find the degree of each polynomial.

7. $4x^2y^3z$
8. $-2abc$
9. $15m$
10. $s + 5t$
11. 22
12. $18x^2 + 4yz - 10y$
13. $x^4 - 6x^2 - 2x^3 - 10$
14. $2x^3y^2 - 4xy^3$
15. $-2r^8s^4 + 7r^2s - 4r^7s^6$
16. $9x^2 + yz^8$
17. $8b + bc^5$
18. $4x^4y - 8zx^2 + 2x^5$
19. $4x^2 - 1$
20. $9abc + bc - d^5$
21. $h^3m + 6h^4m^2 - 7$

Lesson 8-4

NAME ______________________ DATE __________ PERIOD ____

8-4 Study Guide and Intervention *(continued)*

Polynomials

Write Polynomials in Order The terms of a polynomial are usually arranged so that the powers of one variable are in **ascending** (increasing) order or **descending** (decreasing) order.

Example 1 **Arrange the terms of each polynomial so that the powers of x are in ascending order.**

a. $x^4 - x^2 + 5x^3$

$-x^2 + 5x^3 + x^4$

b. $8x^3y - y^2 + 6x^2y + xy^2$

$-y^2 + xy^2 + 6x^2y + 8x^3y$

Example 2 **Arrange the terms of each polynomial so that the powers of x are in descending order.**

a. $x^4 + 4x^5 - x^2$

$4x^5 + x^4 - x^2$

b. $-6xy + y^3 - x^2y^2 + x^4y^2$

$x^4y^2 - x^2y^2 - 6xy + y^3$

Exercises

Arrange the terms of each polynomial so that the powers of x are in ascending order.

1. $5x + x^2 + 6$

2. $6x + 9 - 4x^2$

3. $4xy + 2y + 6x^2$

4. $6y^2x - 6x^2y + 2$

5. $x^4 + x^3 + x^2$

6. $2x^3 - x + 3x^7$

7. $-5cx + 10c^2x^3 + 15cx^2$

8. $-4nx - 5n^3x^3 + 5$

9. $4xy + 2y + 5x^2$

Arrange the terms of each polynomial so that the powers of x are in descending order.

10. $2x + x^2 - 5$

11. $20x - 10x^2 + 5x^3$

12. $x^2 + 4yx - 10x^5$

13. $9bx + 3bx^2 - 6x^3$

14. $x^3 + x^5 - x^2$

15. $ax^2 + 8a^2x^5 - 4$

16. $3x^3y - 4xy^2 - x^4y^2 + y^5$

17. $x^4 + 4x^3 - 7x^5 + 1$

18. $-3x^6 - x^5 + 2x^8$

19. $-15cx^2 + 8c^2x^5 + cx$

20. $24x^2y - 12x^3y^2 + 6x^4$

21. $-15x^3 + 10x^4y^2 + 7xy^2$

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8-5 Study Guide and Intervention

Adding and Subtracting Polynomials

Add Polynomials To add polynomials, you can group like terms horizontally or write them in column form, aligning like terms vertically. **Like terms** are monomial terms that are either identical or differ only in their coefficients, such as $3p$ and $-5p$ or $2x^2y$ and $8x^2y$.

Example 1 **Find $(2x^2 + x - 8) + (3x - 4x^2 + 2)$.**

Horizontal Method

Group like terms.

$(2x^2 + x - 8) + (3x - 4x^2 + 2)$

$= [(2x^2 + (-4x^2)] + (x + 3x) + [(-8) + 2)]$

$= -2x^2 + 4x - 6.$

The sum is $-2x^2 + 4x - 6$.

Example 2 **Find $(3x^2 + 5xy) + (xy + 2x^2)$.**

Vertical Method

Align like terms in columns and add.

$$\begin{array}{rl} & 3x^2 + 5xy \\ (+) & 2x^2 + xy \\ \hline & 5x^2 + 6xy \end{array}$$

Put the terms in descending order.

The sum is $5x^2 + 6xy$.

Exercises

Find each sum.

1. $(4a - 5) + (3a + 6)$

2. $(6x + 9) + (4x^2 - 7)$

3. $(6xy + 2y + 6x) + (4xy - x)$

4. $(x^2 + y^2) + (-x^2 + y^2)$

5. $(3p^2 - 2p + 3) + (p^2 - 7p + 7)$

6. $(2x^2 + 5xy + 4y^2) + (-xy - 6x^2 + 2y^2)$

7. $(5p + 2q) + (2p^2 - 8q + 1)$

8. $(4x^2 - x + 4) + (5x + 2x^2 + 2)$

9. $(6x^2 + 3x) + (x^2 - 4x - 3)$

10. $(x^2 + 2xy + y^2) + (x^2 - xy - 2y^2)$

11. $(2a - 4b - c) + (-2a - b - 4c)$

12. $(6xy^2 + 4xy) + (2xy - 10xy^2 + y^2)$

13. $(2p - 5q) + (3p + 6q) + (p - q)$

14. $(2x^2 - 6) + (5x^2 + 2) + (-x^2 - 7)$

15. $(3z^2 + 5z) + (z^2 + 2z) + (z - 4)$

16. $(8x^2 + 4x + 3y^2 + y) + (6x^2 - x + 4y)$

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8-5 Study Guide and Intervention *(continued)*

Adding and Subtracting Polynomials

Subtract Polynomials You can subtract a polynomial by adding its additive inverse. To find the additive inverse of a polynomial, replace each term with its additive inverse or opposite.

Example **Find $(3x^2 + 2x - 6) - (2x + x^2 + 3)$.**

Horizontal Method

Use additive inverses to rewrite as addition. Then group like terms.

$(3x^2 + 2x - 6) - (2x + x^2 + 3)$

$= (3x^2 + 2x - 6) + [(-2x) + (-x^2) + (-3)]$

$= [3x^2 + (-x^2)] + [2x + (-2x)] + [-6 + (-3)]$

$= 2x^2 + (-9)$

$= 2x^2 - 9$

The difference is $2x^2 - 9$.

Vertical Method

Align like terms in columns and subtract by adding the additive inverse.

$$\begin{array}{rr} & 3x^2 + 2x - 6 \\ (-) & \underline{x^2 + 2x + 3} \end{array}$$

$$\begin{array}{rr} & 3x^2 + 2x - 6 \\ (+) & \underline{-x^2 - 2x - 3} \\ & 2x^2 \qquad - 9 \end{array}$$

The difference is $2x^2 - 9$.

Exercises

Find each difference.

1. $(3a - 5) - (5a + 1)$
2. $(9x + 2) - (-3x^2 - 5)$
3. $(9xy + y - 2x) - (6xy - 2x)$
4. $(x^2 + y^2) - (-x^2 + y^2)$
5. $(6p^2 + 4p + 5) - (2p^2 - 5p + 1)$
6. $(6x^2 + 5xy - 2y^2) - (-xy - 2x^2 - 4y^2)$
7. $(8p - 5q) - (-6p^2 + 6q - 3)$
8. $(8x^2 - 4x - 3) - (-2x - x^2 + 5)$
9. $(3x^2 - 2x) - (3x^2 + 5x - 1)$
10. $(4x^2 + 6xy + 2y^2) - (-x^2 + 2xy - 5y^2)$
11. $(2h - 6j - 2k) - (-7h - 5j - 4k)$
12. $(9xy^2 + 5xy) - (-2xy - 8xy^2)$
13. $(2a - 8b) - (-3a + 5b)$
14. $(2x^2 - 8) - (-2x^2 - 6)$
15. $(6z^2 + 4z + 2) - (4z^2 + z)$
16. $(6x^2 - 5x + 1) - (-7x^2 - 2x + 4)$

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8-6

Study Guide and Intervention

Multiplying a Polynomial by a Monomial

Lesson 8-6

Product of Monomial and Polynomial The Distributive Property can be used to multiply a polynomial by a monomial. You can multiply horizontally or vertically. Sometimes multiplying results in like terms. The products can be simplified by combining like terms.

Example 1 **Find $-3x^2(4x^2 + 6x - 8)$.**

Horizontal Method

$-3x^2(4x^2 + 6x - 8)$

$= -3x^2(4x^2) + (-3x^2)(6x) - (-3x^2)(8)$

$= -12x^4 + (-18x^3) - (-24x^2)$

$= -12x^4 - 18x^3 + 24x^2$

Vertical Method

$$\begin{array}{lr} & 4x^2 + 6x - 8 \\ (\times) & -3x^2 \\ \hline & -12x^4 - 18x^3 + 24x^2 \end{array}$$

The product is $-12x^4 - 18x^3 + 24x^2$.

Example 2 **Simplify $-2(4x^2 + 5x) - x(x^2 + 6x)$.**

$-2(4x^2 + 5x) - x(x^2 + 6x)$

$= -2(4x^2) + (-2)(5x) + (-x)(x^2) + (-x)(6x)$

$= -8x^2 + (-10x) + (-x^3) + (-6x^2)$

$= (-x^3) + [-8x^2 + (-6x^2)] + (-10x)$

$= -x^3 - 14x^2 - 10x$

Exercises

Find each product.

1. $x(5x + x^2)$

2. $x(4x^2 + 3x + 2)$

3. $-2xy(2y + 4x^2)$

4. $-2g(g^2 - 2g + 2)$

5. $3x(x^4 + x^3 + x^2)$

6. $-4x(2x^3 - 2x + 3)$

7. $-4cx(10 + 3x)$

8. $3y(-4x - 6x^3 - 2y)$

9. $2x^2y^2(3xy + 2y + 5x)$

Simplify.

10. $x(3x - 4) - 5x$

11. $-x(2x^2 - 4x) - 6x^2$

12. $6a(2a - b) + 2a(-4a + 5b)$

13. $4r(2r^2 - 3r + 5) + 6r(4r^2 + 2r + 8)$

14. $4n(3n^2 + n - 4) - n(3 - n)$

15. $2b(b^2 + 4b + 8) - 3b(3b^2 + 9b - 18)$

16. $-2z(4z^2 - 3z + 1) - z(3z^2 + 2z - 1)$

17. $2(4x^2 - 2x) - 3(-6x^2 + 4) + 2x(x - 1)$

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8-6 Study Guide and Intervention *(continued)*

Multiplying a Polynomial by a Monomial

Solve Equations with Polynomial Expressions Many equations contain polynomials that must be added, subtracted, or multiplied before the equation can be solved.

Example **Solve $4(n - 2) + 5n = 6(3 - n) + 19$.**

$4(n - 2) + 5n = 6(3 - n) + 19$	Original equation
$4n - 8 + 5n = 18 - 6n + 19$	Distributive Property
$9n - 8 = 37 - 6n$	Combine like terms.
$15n - 8 = 37$	Add $6n$ to both sides.
$15n = 45$	Add 8 to both sides.
$n = 3$	Divide each side by 15.

The solution is 3.

Exercises

Solve each equation.

1. $2(a - 3) = 3(-2a + 6)$

2. $3(x + 5) - 6 = 18$

3. $3x(x - 5) - 3x^2 = -30$

4. $6(x^2 + 2x) = 2(3x^2 + 12)$

5. $4(2p + 1) - 12p = 2(8p + 12)$

6. $2(6x + 4) + 2 = 4(x - 4)$

7. $-2(4y - 3) - 8y + 6 = 4(y - 2)$

8. $c(c + 2) - c(c - 6) = 10c - 12$

9. $3(x^2 - 2x) = 3x^2 + 5x - 11$

10. $2(4x + 3) + 2 = -4(x + 1)$

11. $3(2h - 6) - (2h + 1) = 9$

12. $3(y + 5) - (4y - 8) = -2y + 10$

13. $3(2a - 6) - (-3a - 1) = 4a - 2$

14. $5(2x^2 - 1) - (10x^2 - 6) = -(x + 2)$

15. $3(x + 2) + 2(x + 1) = -5(x - 3)$

16. $4(3p^2 + 2p) - 12p^2 = 2(8p + 6)$

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8-7 Practice

Multiplying Polynomials

Find each product.

1. $(q + 6)(q + 5)$

2. $(x + 7)(x + 4)$

3. $(s + 5)(s - 6)$

4. $(n - 4)(n - 6)$

5. $(a - 5)(a - 8)$

6. $(w - 6)(w - 9)$

7. $(4c + 6)(c - 4)$

8. $(2x - 9)(2x + 4)$

9. $(4d - 5)(2d - 3)$

10. $(4b + 3)(3b - 4)$

11. $(4m + 2)(4m - 3)$

12. $(5c - 5)(7c + 9)$

13. $(6a - 3)(7a - 4)$

14. $(6h - 3)(4h - 2)$

15. $(2x - 2)(5x - 4)$

16. $(3a - b)(2a - b)$

17. $(4g + 3h)(2g + 3h)$

18. $(4x + y)(4x + y)$

19. $(m + 5)(m^2 + 4m - 8)$

20. $(t + 3)(t^2 + 4t + 7)$

21. $(2h + 3)(2h^2 + 3h + 4)$

22. $(3d + 3)(2d^2 + 5d - 2)$

23. $(3q + 2)(9q^2 - 12q + 4)$

24. $(3r + 2)(9r^2 + 6r + 4)$

25. $(3c^2 + 2c - 1)(2c^2 + c + 9)$

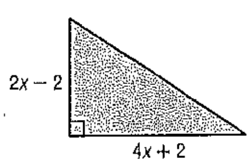
26. $(2\ell^2 + \ell + 3)(4\ell^2 + 2\ell - 2)$

27. $(2x^2 - 2x - 3)(2x^2 - 4x + 3)$

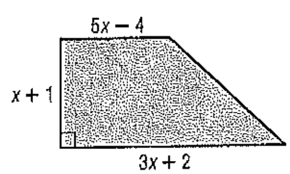
28. $(3y^2 + 2y + 2)(3y^2 - 4y - 5)$

GEOMETRY **Write an expression to represent the area of each figure.**

29.



30.



31. NUMBER THEORY Let x be an even integer. What is the product of the next two consecutive even integers?

32. GEOMETRY The volume of a rectangular pyramid is one third the product of the area of its base and its height. Find an expression for the volume of a rectangular pyramid whose base has an area of $3x^2 + 12x + 9$ square feet and whose height is $x + 3$ feet.

8-8 Study Guide and Intervention

Special Products

Squares of Sums and Differences Some pairs of binomials have products that follow specific patterns. One such pattern is called the *square of a sum*. Another is called the *square of a difference*.

Square of a sum	$(a + b)^2 = (a + b)(a + b) = a^2 + 2ab + b^2$
Square of a difference	$(a - b)^2 = (a - b)(a - b) = a^2 - 2ab + b^2$

Example 1 **Find $(3a + 4)(3a + 4)$.**

Use the square of a sum pattern, with $a = 3a$ and $b = 4$.

$$(3a + 4)(3a + 4) = (3a)^2 + 2(3a)(4) + (4)^2$$
$$= 9a^2 + 24a + 16$$

The product is $9a^2 + 24a + 16$.

Example 2 **Find $(2z - 9)(2z - 9)$.**

Use the square of a difference pattern with $a = 2z$ and $b = 9$.

$$(2z - 9)(2z - 9) = (2z)^2 - 2(2z)(9) + (9)(9)$$
$$= 4z^2 - 36z + 81$$

The product is $4z^2 - 36z + 81$.

Exercises

Find each product.

1. $(x - 6)^2$

2. $(3p + 4)^2$

3. $(4x - 5)^2$

4. $(2x - 1)^2$

5. $(2h + 3)^2$

6. $(m + 5)^2$

7. $(c + 3)^2$

8. $(3 - p)^2$

9. $(x - 5y)^2$

10. $(8y + 4)^2$

11. $(8 + x)^2$

12. $(3a - 2b)^2$

13. $(2x - 8)^2$

14. $(x^2 + 1)^2$

15. $(m^2 - 2)^2$

16. $(x^3 - 1)^2$

17. $(2h^2 - k^2)^2$

18. $\left(\frac{1}{4}x + 3\right)^2$

19. $(x - 4y^2)^2$

20. $(2p + 4q)^2$

21. $\left(\frac{2}{3}x - 2\right)^2$

Lesson 8-8

NAME ______________________ DATE ________ PERIOD _____

8-8 Study Guide and Intervention *(continued)*

Special Products

Product of a Sum and a Difference There is also a pattern for the product of a sum and a difference of the same two terms, $(a + b)(a - b)$. The product is called the **difference of squares.**

Product of a Sum and a Difference	$(a + b)(a - b) = a^2 - b^2$

Example **Find $(5x + 3y)(5x - 3y)$.**

$(a + b)(a - b)$	$= a^2 - b^2$	Product of a Sum and a Difference
$(5x + 3y)(5x - 3y)$	$= (5x)^2 - (3y)^2$	$a = 5x$ and $b = 3y$
	$= 25x^2 - 9y^2$	Simplify.

The product is $25x^2 - 9y^2$.

Exercises

Find each product.

1. $(x - 4)(x + 4)$

2. $(p + 2)(p - 2)$

3. $(4x - 5)(4x + 5)$

4. $(2x - 1)(2x + 1)$

5. $(h + 7)(h - 7)$

6. $(m - 5)(m + 5)$

7. $(2c - 3)(2c + 3)$

8. $(3 - 5q)(3 + 5q)$

9. $(x - y)(x + y)$

10. $(y - 4x)(y + 4x)$

11. $(8 + 4x)(8 - 4x)$

12. $(3a - 2b)(3a + 2b)$

13. $(3y - 8)(3y + 8)$

14. $(x^2 - 1)(x^2 + 1)$

15. $(m^2 - 5)(m^2 + 5)$

16. $(x^3 - 2)(x^3 + 2)$

17. $(h^2 - k^2)(h^2 + k^2)$

18. $\left(\frac{1}{4}x + 2\right)\left(\frac{1}{4}x - 2\right)$

19. $(3x - 2y^2)(3x + 2y^2)$

20. $(2p - 5s)(2p + 5s)$

21. $\left(\frac{4}{3}x - 2y\right)\left(\frac{4}{3}x + 2y\right)$

Name: ______________________________ Date: __________

Solving Exponential Equations with Different Bases.

Solve each equation for the variable.

1. $9^{2x-1} \cdot 9^{x+2} = 9^8$

2. $3^{3x} \cdot 3^{2x-1} = \frac{3^{4x+7}}{3^{2x-1}}$

3. $\frac{7^{3x+4}}{7^{x-3}} = 1$

4. $\left(\frac{5^{7x+4}}{25^{3x-3}}\right)^2 = 125^{x+2}$

5. $(6^x \cdot 36^{2x-2})^3 = 6$

6. $\left(\frac{9^{2x-1}}{9^{x+4}}\right)^2 = 9^{3x-1}$

7. $8^{3x+4} \cdot 2^{6-x} = \frac{4^{3x}}{16^{x+1}}$

8. $5 \cdot 5^{3x} = 5^{5x-7}$